# Still At Risk 

## Mathematics

 in the $U S$
## A Nation At Risk

"We are at risk of becoming a nation divided both economically and racially by knowledge of mathematics."
"By the year 2000, United States students will be first in the world in mathematics and science achievement."

-National Education Goal \#5

# Achievement In K-12 

## Results on International Assessments

## TIMSS Nations’ Average Mathematics Performance Compared With the US

Nations Scoring


## Average Mathematics Performance of Advanced Mathematics Students in All TIMSS Countries



Source: NCES, TIMSS, Pursuing Excellence: A Study of US Twelfth-Grade Mathematics and Science Achievement in International Context, 1999.

## Nations’ Average Mathematics Science Performance Compared With the US on PISA

Nations Scoring


# One measure on which we're near the top on PISA? 

## Inequality!

## Performance Of US 15 Year-Olds Highly Variable

|  | PISA 5 <br> th_-95 <br> Gap Rank $^{*}$ |
| :--- | :---: |
| Reading (interpreting texts) | 3 |
| Mathematical Literacy | 6 (tie) |
| Science Literacy | 7 |

## *Of 27 OECD countries

Source: OECD, Knowledge and Skills for Life: First Results From PISA The 2000, 2001.

## Inside the US

## ... a look at NAEP results

# Results Up at All Grade Levels 

## National Mathematics Scale Score Results: 1990-2000 4th Graders Show Most Gains

Nation



Source: National Center for Education Statistics, National Assessment of Educational Progress (NAEP), 1990, 1992, 1996, and 2000 Mathematical Assessments.

# Unlike in previous decades, when minorities made greater gains, gaps remained wide during nineties. 

Gaps Narrow, Then Hold Steady or Widen: NAEP Math Scores, 13 Year-Olds


Source: US Department of Education, National Center for Education Statistics. NAEP 1999 Trends in Academic Progress (p. 180 The
Washington, DC: US Department of Education, August 2000

## Gaps Narrow, Then Hold Steady or Widen: NAEP Math Scores, 17 Year-Olds



Source: US Department of Education, National Center for Education Statistics. NAEP 1999 Trends in Academic Progress (p. 108) Washington, DC: US Department of Education, August 2000

# Despite progress, few students proficient or advanced... and too many performing below even the basic level. 

## NAEP Mathematics Performance 2000



Source: US Department of Education, NEAP Mathematics 2000.

## 8th Graders Performing Below Basic in Mathematics 2000



Source: US Department of Education, NEAP Mathematics 2000.

## 12th Graders Performing Below Basic in Mathematics 2000



Source: US Department of Education, NEAP Mathematics 2000.

## High schools a special problem

## Students Make More Growth In Grades 5-8 Than 9-12, Class of '00



Source: US Department of Education, NEAP Mathematics 2000.

## Value Added Declining in High School Math

Age 13-17 Growth

$\square$ Class of '90 ■Class of '94 ■Class of '96 $\square$ Class of '00
Source: US Department of Education, NEAP Mathematics 2000.

## Skills at end of high school?

## Too Few 17 Year-Olds Demonstrate Strong Math Skills

|  | African <br> American | Latino | White |
| :--- | :---: | :---: | :---: |
| Multi-Step <br> Problem Solving, <br> Algebra | $\mathbf{1 \%}$ | $\mathbf{3 \%}$ | $\mathbf{1 0 \%}$ |
| Moderately <br> Complex <br> Procedures | 27 | 38 | $\mathbf{7 0}$ |
| Numerical <br> Operations | $\mathbf{8 9}$ | $\mathbf{9 4}$ | $\mathbf{9 9}$ |

## African American and Latino 17 Year Olds Do Math at Same Leyels As White 13 Year Olds



# Achievement in Higher Education 

## Many College Graduates Demonstrate Weak Quantitative Literacy Skills

|  | Grads: <br> 2 Yr. Colleges | $\begin{gathered} \text { Grads: } \\ 4 \text { Yr. Colleges } \end{gathered}$ |
| :---: | :---: | :---: |
| Level 5: High | 5 | 13 |
| Level 4 | 30 | 40 |
| Level 3 | 44 | 40 |
| Level 2 | 17 | 10 |
| Level 1: Low | 4 | 3 |

Source: USDOE, NCES, National Adult Literacy Survey, 1992, in Literacy in the Labor Force: Results from the NALS, September 1999, p. 61.

## Description: Quantitative Literacy Level 2

- CAN Calculate postage and fees for certified mail
- CAN Determine difference in price between tickets for

- CAN'T Calculate difference between regular and sale price from an advertisement using a calculator
- CAN'T Plan travel arrangements for meeting using flight schedule

Source: USDOE, NCES, National Adult Literacy Survey, 1992, in Literacy in the Labor Force: Results from the NALS, September 1999, p. 15.

## Description: Quantitative Literacy Level 3

- CAN Determine correct change using information on a menu
- CAN Use information stated in news article to calculate amount of money it takes to raise a child
- CAN'T Determine shipping and total costs on an order form for items in a catalog
- CAN'T Use information in news article to calculate difference in time for completing a race


## Gaps between groups?

## Colleges Don’t Close Gaps

|  | Highest <br> Education | White <br> Black Gap | White <br> Hispanic Gap |
| :---: | :---: | :---: | :---: |
| Quantitative | HS <br> Diploma | 47 | 39 |
|  | 2 Year <br> Degree | 46 | 27 |
|  | 4 Year <br> Degree | 49 | 43 |

Source: USDOE, OERI, Adult Literacy in America: A First Look at the Results of the Results of the National Adult Literacy Survey (NALS), 1992, September 1993, p. 36.

## How do our skills compare internationally?

## Almost Half of US Adults Perform at Lowest Literacy Levels in All Areas

| Literacy Scale | Level 1 <br> $(0-225)$ | Level 2 <br> $(226-275)$ | Level 1 + 2 <br> $(0-275)$ |
| :--- | :---: | :---: | :---: |
| Prose | $\mathbf{2 1 \%}+\mathbf{2 6 \%}$ | $\mathbf{4 7 \%}$ |  |
| Document | $\mathbf{2 4 \%}$ | $\mathbf{2 6 \%}$ | $\mathbf{5 0 \%}$ |
| Quantitative | $\mathbf{2 1 \%}$ | $\mathbf{2 5 \%}$ | $\mathbf{4 6 \%}$ |
| Composite | $\mathbf{2 0 \%}$ | $\mathbf{2 5 \%}$ | $\mathbf{4 5 \%}$ |

(score range in parenthesis)

Source: Andrew Sum, Irwin Kirsch, and Robert Taggart. The Twin Challenges of Mediocrity and an International Perspective. Policy Information Center, Educational Testing Service. (2002)

## College Degrees Don't Fix the Problem: US Adults Rank Poorly Among 20 High-Income Countries

| Educational Attainment | Quantitative <br> Scale |
| :--- | :---: |
| High-School Grad/GED, no <br> college | 19 th |
| $1-3$ yrs of college | 17 th |
| Bachelor's degree or higher | 13th |

## Mathematics Education

# "Mathematics and science education will be strengthened throughout the system, especially in the early grades. 

-National Education Goal \#5, Objective 1

## CURRICULUM: <br> K-12

# 8th Grade: A lot of crossnational information because of TIMSS 



## Quality of Mathematical Content of 8th Grade Lessons



Source: TIMSS : unpublished tabulations, Videotape Classroom Study, UCLA, 1996, in Pursuing Excellence: A Study of US Eigth-Grade Mathematics and Science Teaching, Learning, Curriculum and Achievement in International Context, 1997.

## Average Grade Level of Content

 in 8th Grade Lessons, by International Standards

Source: NCES, "Pursuing Excellence: A Study of US Eighth-Grade Mathematics and Science Teaching, Learning, Curriculum, and Achievement in International Context", 1997.

## Algebra In 8th Grade Text Books

\% Of Space Devoted To Algebra In 8th Grade Mathematics Textbooks


Source: NCES, "Pursuing Excellence: A Study of US Eighth-Grade Mathematics and Science Teaching, Learning, Curriculum, and Achievement in International Context", 1997.

## Math Emphasis Favors Routine Skills Over Understanding

United States 8th Grade Math Teachers


| $\square$ Goal = |
| :--- |
| Mathematical |
| thinking |
| $\square$ Goal = Learn |
| skill/formula |
|  |
| $\square$ Practice routine |
| procedures |
|  |
| $\square$Invent new <br> solutions and <br> proofs |

Source: Pursuing Excellence: A Study of US Eigth-Grade Mathematics and Science Teaching, Learning, Curriculum and Achievement in International Context, 1997.

# High School: Moving More Students into College-Prep Math Sequence 

## High School Graduates Taking More Mathematics



## Percentage of High School Graduates Completing Algebra II, 1998



## Percentage of High School Graduates Completing Pre-calculus, 1998



Source: HS\&B, HSTS, NELS data, in NCES, Digest of Education Statistics, 2000.

## Percentage of High School Graduates Completing Calculus, 1998



Source: HS\&B, HSTS, NELS data, in NCES, Digest of Education Statistics, 2000.

# CURRICULUM: Higher Education 

## UNDERGRADUATE MATHEMATICS COURSE ENROLLMENT

㕩 Enrollments in mathematical sciences courses doubled in the 70 s and 80 s, but the increases were all at the lower levels, with remedial enrollments leading the way.

[^0]
## Undergraduate Mathematics Course Enrollment

- Even at top rated doctoral granting public universities*, nearly $20 \%$ of total student enrollment in mathematics is at the Remedial or Precalculus levels.
*Group IA

Source: Towards Excellence: Leading a Mathematics Department in the 21st Century, American Mathematical Society, 2001.

## Many Freshmen Must Take Remedial Math Courses, 1995

| All institutions | $\mathbf{2 4 \%}$ |
| :--- | :--- |
| Public 2 year | $\mathbf{3 4 \%}$ |
| Public 4 year | $\mathbf{1 8 \%}$ |
| High Minority <br> Enrollment | $\mathbf{3 5 \%}$ |
| Low Minority <br> Enrollment | $\mathbf{2 1 \%}$ |

## TEACHERS: K-12

# "The number of teachers with a substantive background in math and science will increase by 50\%" 

-National Education Goal \#5, Objective 2

## How Far Have We Come?

Percentage Public High School Math Teachers With Major or Minor in Field


Source: Richard M. Ingersoll, "The Problem of Underqualified Teachers in American Secondary Schools," Education The Education Researcher, Vol. 28, Number 2, March 1999

## International Problem?

## Who Teaches Grade 8 Mathematics?

## $\square$ US ■ International Average



Source: ISDPE, OERI, Pursuing Excellence: Comparison of International EighthGrade Mathematics and Science Achievement from a US Perspective, 1999, 2001.

If teachers without sufficient content are a problem, that problem affects different groups of students differently.

## Percent High School Math Classes Whose Teachers Have No Major or Minor in Math



Source: Schools and Staffing Survey 1999-2000, calculations by Richard Ingersoll for the the Education Trust, 2002.

## Percent Middle School Math Classes Whose Teachers Have No Major or Minor in Math



Source: Schools and Staffing Survey 1999-2000, calculations by Richard Ingersoll for the the Education Trust, 2002.

## Teachers in general compared to other BA's?

## Math Literacy of Teachers Versus Other BAs



Source: ETS, Barbara A. Bruschi and Richard J. Coley, "How Teachers Compare: The Prose, Document and Quantitative Skills of America's Teachers", Princeton, NJ, 1999, p. 6.

## Description: Quantitative Literacy Level 3

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## TEACHERS: Higher Education

## Who Is Teaching Remedial Mathematics?



Source: Fall 1995 Conference Board Mathematical Sciences Survey

## Who's Teaching Freshman Mathematics In Research Universities?



Source: Fall 1995 Conference Board Mathematical Sciences Survey

# Where are the Math Majors? 

"The number of US undergraduate and graduate students, especially women and minorities, who complete degrees in mathematics, science, and engineering, will increase significantly."
-National Education Goal \#5, Objective 3

## Junior/Senior Mathematical Sciences Majors Declining



Source: 1999 Annual Survey of the Mathematical Sciences (Second Report), AMS, Vol. 47, Number 8.

## Math Degrees Declining, 1971-2000



Source: US Department of Education, NCES, Digest of Education Statistics, 2001, Tables 257.

## 1997-98 Bachelor's Degrees Awarded In Mathematics



- White
- Black

■ Hispanic
■ Asian/Pacific-Islander Non-residents

## 1997-98 Master's Degrees Awarded In Mathematics



| $\square$ White |
| :--- |
| $\square$ Black |
| $\square$ Hispanic |
| $\square$ Asian/Pacific/Islander |
| $\square$ Non-Resident |

## 1994-95 Doctor's Degrees Awarded In Mathematics



| $\square$ White |
| :--- |
| $\square$ Black |
| $\square$ Hispanic |
| $\square$ Asian/Pacific Islander |
| $\square$ Non-resident |

NCES, Digest of Education Statistics 1997.

## MATH TEACHER DEMAND

## Shortage of Certified and Fully Qualified Math Teachers



Source: NCES, SASS data, in Before It's Too Late: A Report to the Nation from the National Commission on Mathematics and Science Teaching for the 21st Century, 2000.

## Demand is Far Outpacing Supply

- An estimated 240,000 middle and high school mathematics and science teachers will be needed over the next 10 years.
- Of this total, nearly $70 \%$ will be newcomers to the profession.

Source: Before It's Too Late: A Report to the Nation from the National Commission on Mathematics and Science Teaching for the 21st Century, 2000.

## Over a Decade...

We might produce as many as 120,000 math MAJORS. BUT, we may have to fill upwards of 130,000 math teaching positions.

# And in the 1990s, only about 29\% of mathematics majors taught at either level, with only about 15\% teaching at any time. 

## Ways OUT

## 1. Start with the data-especially YOUR data.

## 2. Provide Assistance to Current Teachers

- Identify most important standards;
- refocus curriculum, assessment and professional development on most important standards


## 3. Increase number of students

 studying mathematics at all levels.- Make college prep curriculum the default curriculum for all students;
- Accelerate students with weak skills BEFORE they take the course, not after they fail;
- Raise requirements for teaching, especially at middle school level;
- Mine ALL sources for teachers with strong math background
- Enroll strongest students in college math, rather than AP;
- Teach "remedial" math in high school



## 4. In higher education?

- Goals, incentives, rewards for increased production of bachelors degrees in math;
- Engage mathematics faculties in strategizing about how to produce more and better teachers of mathematics;
--- Work on the mathematical literacy of ALL college students.


# The Education Trust 

www.edtrust.org 202-293-1217


[^0]:    Committee on the Mathematical Sciences in the Year 2000, A Challenge of Numbers: People in the Mathematical Sciences. National Academy Press: Washington, D.C., 1990.

